International Trade and Macro: Sunk-cost models

#### Model outline

- 1. CES + monopolistic competition math
- 2. Firm decision problem in partial equilibrium
- 3. Success and challenges

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# CES + monopolistic competition: Consumers

- ▶ m<sub>i</sub> mass of varieties available
- ► Total expenditure *E* exogenous but time-varying

$$\max_{\boldsymbol{c}(\nu)>0} \left( \int_0^m \omega_t(\nu) \boldsymbol{c}(\nu)^{\frac{\theta-1}{\theta}} d\nu \right)^{\frac{\theta}{\theta-1}}$$
s.t. 
$$\int_0^m \boldsymbol{p}(\nu) \boldsymbol{c}(\nu) d\nu = E_t$$

Demand function

$$d(\nu, p) = \omega_t(\nu)^{\theta} \left(\frac{p(\nu)}{P_t}\right)^{-\theta} \frac{E_t}{P_t}$$

- $\blacktriangleright$  Price of  $\nu$  relative to aggregate price
- ightharpoonup Price elasticity of demand  $\theta$

# CES + monopolistic competition: Variety producers

- Monopolistic competitors: not monopolists, but some market power
- Choose prices taking residual demand as given (atomistic)
- Linear (generally CRS) production
- ▶ Variable trade costs:  $\tau_t \ge 1$  = tariffs;  $\xi_t$  = common trade cost;  $\hat{\xi}_t(\nu)$  = idio trade cost

$$\max_{p,l} p(\nu)d(\nu,\tau p) - wl(\nu)$$
  
s.t.  $\xi_l \hat{\xi}_l(\nu)d(\nu,\tau p) = z_l(\nu)l(\nu)$ 

► The ex-tariff pricing decision

$$p(\nu) = \frac{\theta}{\theta - 1} \frac{w}{z_t(\nu)} \xi_t \hat{\xi}_t(\nu)$$

- ▶ Markup decreasing in  $\theta > 1$  (Why?)
- ▶ Better firms charge lower prices

# CES + monopolistic competition: Variety producers

▶ Substitute price and labor demand functions into the objective

$$p(\nu)c(\nu) = E_t P_t^{\theta-1} \omega_t(\nu)^{\theta} \left( \frac{\theta}{\theta-1} \frac{\mathbf{w}}{\mathbf{z}_t} \tau_t \xi_t \hat{\xi}_t(\nu) \right)^{-(\theta-1)}$$

▶ and profits...

$$\pi(\nu) = \frac{1}{\theta} p(\nu) c(\nu)$$

▶ These are very special properties of CES + monop. competition

- ▶ Notice that  $p, c, \pi$  do not depend on  $\nu$ . They depend on  $z, \hat{\xi}$ , and  $\omega$ .
- ▶ Index goods by  $(z, \hat{\xi}, \omega)$  and use the measure over them to aggregate.

# Static "entry" model intuition

## Sunk-cost model: decision problem

- Now we introduce the sunk-cost model, sometimes with a more general notation
- ▶ Three key features in firm-level models of trade
  - 1. An investment in "market access" technology
  - 2. An uncertain future return to that investment
  - 3. A depreciation process of that investment

# Sunk-cost model: decision problem

▶ Consider a firm *i* making a decision to export:  $x_{it} = \{0, 1\}$ 

$$V_t = \max E_t \sum_{s=t}^{\infty} \frac{1}{1+r_s} X_{is} \left( \pi_{is} \left( \cdot \right) - f_{is} \left( \cdot \right) \right)$$

- ► Fixed export costs:  $f_{it}(\epsilon_{it}, x_{it-1}, x_{it-2}, ..., x_{it-k})$  depend on random variable and experience
- ▶ Flow profits:  $\pi(x_{it}, z_{it}, d_{it})$ 
  - $ightharpoonup z_{it}$  = variables related to productive efficiency
  - $ightharpoonup d_{it}$  = variables related to foreign demand for firm i's
  - ▶ Assumes constant returns to scale, otherwise  $z_{it}$  ( $s_{it}$ ,  $d_{it}$ ) where  $s_{it}$  is sales at home

# Model: foreign demand

Assume a firm charging price p<sub>it</sub> sells

$$d_{it}\left(p_{it}\right) = \omega_{it}\left(p_{it}\frac{\tau_{t}\xi_{t}\tilde{\xi}_{it}}{P_{t}}\right)^{-\theta}D_{t}$$

- ▶ Common factors: market size  $(D_t)$ , real exchange rate  $(P_t)$ , ad-valorem tariff  $(\tau_t)$ , iceberg trade costs  $(\xi_t)$
- ▶ Idiosyncratic factors: demand shifter  $(\omega_{it})$  and  $\left(\tilde{\xi}_{it}\right)$  e.g., shipping/distribution technology
  - ▶ Two idiosyncratic factors redundant, combine into  $\xi_{it}$
  - ▶ No congestion effects on distribution
- CES framework is common

#### Fixed costs

- ► Following Baldwin and Krugman (1989); Roberts and Tybout (1997)
- ▶  $f(\epsilon_{it}, x_{it-1})$ : only t-1 export status matters (full depreciation of market-access investment)
- ▶  $f(\epsilon_{it}, 1) < f(\epsilon_{it}, 0)$ : cost of entering exceeds continuation cost (upfront investment in market access)
- ▶ fixed cost lowers iceberg cost from  $\xi = \infty$  to  $\xi < \infty$  (return on investment)
- When fixed trade cost only depends on last period's export status the fixed cost and history variable are redundant.
- ➤ A richer model in which fixed costs depend on experience requires tracking longer history

# Uncertainty

- ▶ Microeconomic  $(z, \xi, f(\epsilon_{it}, x_{it-1}))$ 
  - ▶ Let  $z, \xi$  follow AR1 process  $\left(\rho_z, \sigma_z^2, \rho_\xi, \sigma_\xi^2\right)$
  - ▶ Fixed cost component follow  $\epsilon_{it} \sim \log \text{Normal}\left(0, \sigma_{\epsilon}^2\right)$
  - ▶ Often assume aspect of  $\xi$  is learned upon entry (Learning)
- ▶ Macroeconomic
  - ▶ Processes for exchange rate (P<sub>t</sub>) & demand (D<sub>t</sub>) depend on equilibrium concept
  - $\blacktriangleright$  In partial equilibrium (P, D) are exogenous AR processes
  - ▶ In general equilibrium, (*P*, *D*) depend on shocks and transmission (can be highly non-linear)
  - For tariffs no standard

# Bellman Equation

► The firm solves a standard discrete-choice problem

$$V_{t}(x_{it-1}, z_{it}, \xi_{it}, f_{it}) = \max \left\{ V_{t}^{0}(x_{it-1}, z_{it}, \xi_{it}, f_{it}), V_{t}^{1}(x_{it-1}, z_{it}, \xi_{it}, f_{it}) \right\}$$

- ▶ To solve this problem we will need to know
  - ▶ A firm's survival probability  $(\delta_{it})$
  - ▶ The interest rate  $(r_t)$
- ▶ The ts capture non-stationary functions from aggregate shocks
  - Most partial equilibrium models assume stationarity

# Bellman Equation

Value of not exporting

$$V_{t}^{0}(x_{it-1}, z_{it}, \xi_{it}, f_{it}) = \pi_{t}(0, z_{it}, \xi_{it}) + \delta_{it} \mathop{\mathsf{E}}_{z, \xi, f} \frac{1}{1 + r_{t+1}} V_{t+1}(0, z_{it+1}, \xi_{it+1}, f_{it+1})$$

▶ Value of exporting

$$V_{t}^{1}(x_{it-1}, z_{it}, \xi_{it}, f_{it}) = \pi_{t}(1, z_{it}, \xi_{it}) - f(\epsilon_{t}, x_{i,t-1}) + \delta_{it} \mathop{\mathsf{E}}_{z, \xi, f} \frac{1}{1 + r_{t+1}} V_{t+1}(1, z_{it+1}, \xi_{it+1}, f_{it+1})$$

► Focus on a stationary environment for now (drop *ts*)

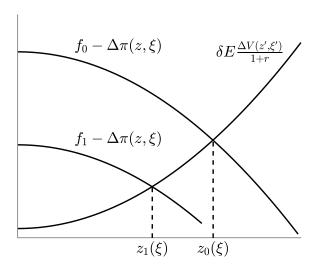
#### **Decision Rules**

- ▶ Assume 1) f is deterministic (i.e.  $\sigma_{\epsilon} = 0$ ) and 2) export and domestic profit increasing in z
- ▶ Optimal policy is a cutoff rule  $z_m(\xi)$  s.t.  $x_{it} = 1$  iff  $z \ge z_m(\xi)$

$$f_{m} - [\pi(1, z_{m}(\xi), \xi) - \pi(0, z_{m}(\xi), \xi)] = \frac{\delta}{1 + r} E \begin{bmatrix} V^{1}(z', \xi', f_{1}) \\ -V^{0}(z', \xi', f_{0}) \end{bmatrix}$$
$$f_{m} - \Delta \pi(z_{m}(\xi), \xi) = \frac{\delta}{1 + r} E [\Delta V(z', \xi', f_{1}, f_{0})]$$

- ► The LHS is the current cost of exporting net of increased profits
- ► The RHS is the future benefit (increase in market value of the firm)

#### Breakevens



# The gain in firm value from exporting

- ► The RHS of the break-even condition
- ▶ The upward sloping line in the figure
- Depends on fixed costs and persistence of shock
- ► The slope is increasing in the persistence of shocks
  - ▶ It determines both how long and how much you earn exporting
- ▶ The intercept is mostly determined by the gap between  $f_0 f_1$ 
  - ▶ If  $f_0 = f_1$  then  $\Delta V = 0$
  - ▶ Holding  $f_1$  constant,  $\frac{\partial \Delta V}{\partial f_0} > 0$

# The current cost of exporting

- ▶ The LHS of the break-even condition
- ► The downward sloping lines in the figure
- ▶ Holding fixed  $\xi$  cost decreases in z
  - ► Exporting more profitable to more productive firms

#### Distributions

- ► The cutoff thresholds and the process for  $(z, \xi)$  determine the measure of firm types  $\mu(z, \xi, f)$
- $\mu$  (z,  $\xi$ , f<sub>0</sub>) [ $\mu$  (z,  $\xi$ , f<sub>1</sub>)] denotes the beginning of period non-exporters [exporters]
- ► The measures of current nonexporters and exporters

$$N_{N} = \int_{\xi}^{z_{0}(\xi)} \int_{0}^{z_{0}(\xi)} \mu(z, \xi, f_{0}) + \int_{\xi}^{z_{1}(\xi)} \int_{0}^{z_{1}(\xi)} \mu(z, \xi, f_{1})$$

$$N_{X} = \int_{\xi} \int_{z_{0}(\xi)}^{\infty} \mu(z, \xi, f_{0}) + \int_{\xi} \int_{z_{1}(\xi)}^{\infty} \mu(z, \xi, f_{1})$$

▶ The export participation share is  $N_X/(N_N+N_X)$ 

#### Laws of motion

$$N_X' = \delta_{X,X} \Pr (\text{continue}) N_X + \delta_{N,X} \Pr (\text{start}) N_N$$

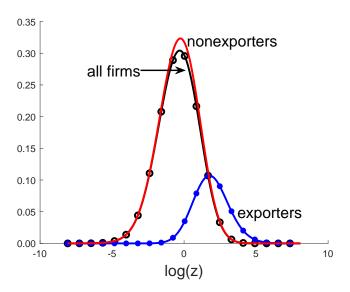
$$N_N' = \delta_{X,N} \left[ 1 - \Pr\left( \text{continue} \right) \right] N_X + \delta_{NN} \left[ 1 - \Pr\left( \text{start} \right) \right] N_N + N_E$$

A more careful exposition would focus fully on

$$\mu'(z,\xi,f) = T(\mu(z,\xi,f))$$

▶ See the appendix to Alessandria et al. (2021a) for details

# **Distributions**



# **Properties**

- ▶ Crucial outcome of dynamic decision:  $z_1(\xi) < z_0(\xi)$ 
  - Harder to break into exporting than to stay
- ▶ This generates
  - Exporter hysteresis: Firms continue exporting after conditions deteriorate
  - ► Low exit rate: Exporters will delay exiting to avoid paying the entry cost again
  - ▶ Export Premium: Exporters are larger than nonexporters
    - Increasing in the average fixed cost
    - Falling in the difference in fixed costs

# **Properties**

- ► Consider impact of changes in current and future primitives abstracting from GE interactions
- ► Let's look at
  - 1. Trade barriers
  - 2. Uncertainty

#### Trade costs and Tariffs

- ▶ Consider three possible reductions in variable trade costs, either  $(\xi, \tau)$ 
  - 1. Current trade costs temporary
  - **2.** Future trade costs permanent
  - 3. Current and future trade costs

# Temporary current

- ▶ Experiment:  $\tau_t \downarrow$ ,  $\tau_s = \tau_{t-1}$ , s = t+1, t+2, ...
- ▶ Lowering today's tariff will shift down the LHS $_m(z)$
- ► Increasing entry and decreasing exit
- ► Through law of motion, trade will remain persistently high, only gradually mean-reverting

#### Permanent future

- ▶ Lowering tariff in the future will shift up the RHS $_m(z)$
- Increasing entry and decreasing exit today
- ► Trade grows in advance of liberalization
- Through law of motion trade will increase gradually

#### Permanent current

- ▶ Lowering tariff in the current will shift up the RHS<sub>m</sub>(z) and LHS<sub>m</sub>(z)
- Combination of previous two shocks
- Increasing entry and decreasing exit today
- ► Trade grows by more on impact
- ► Through law of motion trade will increase gradually.

#### Uncertainty

- ➤ As in typical models with non-convexities, uncertainty matters (Dixit and Pindyck, 1994)
- **1.** Current dispersion in productivity,  $\sigma_z \uparrow$  [temporary]
  - Does not affect thresholds, but does affect distribution of ability today
  - ► Thicker tails → more entry and more exit
  - Volume of trade should increase since conditional mean of productivity ↑ (selection on a thicker right tail)
- **2.** Future uncertainty/dispersion,  $\sigma'_z \uparrow$  [permanent]
  - Shift up and flattening of the marginal gain curve
  - Entry and exit fall, ambiguous effect on trade today and in the future

# Success and Challenges

#### Successes

- Persistent export participation (fact #1)
- ► Low export and entry rates (facts #3,4)
- ▶ Dynamic macro adjustment (fact #7)

#### ▶ Challenges

- New exporters (too productive at entry, too likely to continue, and export intensity too high)
- ► Connection in exporting across markets
- ▶ High re-entry rates in monthly and longer frequencies

#### Causes

- ▶ Exporting technology too simple (parsimonious):  $f_0, f_1, \xi$
- Need to shift more investment into post-entry period and reduce depreciation

# Resolutions: Starting and stopping

- ► Small new-exporters & low continuation rate
  - ▶ Let  $f_1(t_e)$  be a decreasing function of  $t_e$ =age in market
- ▶ High re-entry data
  - ▶ Annual: Let firm that stops re-enter with  $f_R \in [f_1, f_0]$
  - ▶ Monthly: set  $f_0 = f_1$ , hold goods in inventories at a cost abroad

# Resolution: Export intensity dynamics

#### With CES

$$exs(z,\hat{\xi}) = \frac{(\tau\xi\hat{\xi})^{1-\sigma}}{1+(\tau\xi\hat{\xi})^{1-\sigma}}$$

- Modify iceberg cost structure so that they fall with experience
  - ► Alessandria et al. (2021b) assume firm enters at  $\xi_H > \xi_L$  and then Markov transition between states
  - ▶ Reflects improvements in export distribution technology
- ► Alternatively could accumulate customers or build habit (Fitzgerald et al., 2016; Piveteau, 2021; Ruhl and Willis, 2017; Rodrigue and Tan, 2019)
- Both approaches have investments in improving market after entry, not just maintaining access
- ▶ Backloads profits which leads to lower estimates of entry costs.
- ▶ When growth process is uncertain, this makes it more likely to exit

#### References

- Alessandria, George, Costas Arkolakis, and Kim J. Ruhl (2021a). "Firm Dynamics and Trade." Annual Review of Economics 13 (1), pp. 253–280.
- Alessandria, George, Horag Choi, and Kim J. Ruhl (2021b). "Trade adjustment dynamics and the welfare gains from trade." *Journal of International Economics* 131, pp. 1034–58.
- Baldwin, Richard E. and Paul R. Krugman (1989). "Persistnent Trade Effects of Large Exchange Rate Shocks." *Quarterly Journal of Economics* 104 (4), pp. 635–54.
- Dixit, Avinash K. and Robert S. Pindyck (1994). *Investment under Uncertainty*. Princeton University Press
- Fitzgerald, Doireann, Stefanie Haller, and Yaniv Yedid-Levi (2016). "How exporters grow." NBER Working Paper 21935.
- Piveteau, Paul (2021). "An empirical dynamic model of trade with consumer accumulation." AEJ: Macro, forthcoming.
- Roberts, Mark J. and James R. Tybout (1997). "The decision to export in Colombia: An empirical model of entry with sunk costs." American Economic Review 87 (4), pp. 545–564.
- Rodrigue, Joel and Yong Tan (2019). "Price, product quality, and exporter Dynamics: Evidence from China." *International Economic Review* 60 (4).
- Ruhl, Kim J. and Jonathan L. Willis (2017). "New exporter dynamics." *International Economic Review* 58 (3), pp. 703–726.