International Trade and Macro:
Sunk-cost models

Model outline

1. Firm decision problem in partial equilibrium
2. Success and challenges

Static “entry” model intuition

Sunk-cost model: decision problem

- Now we introduce the sunk-cost model, sometimes with a more general notation
- Three key features in firm-level models of trade
  1. An investment in “market access” technology
  2. An uncertain future return to that investment
  3. A depreciation process of that investment

Sunk-cost model: general decision problem

- Consider a firm i making a decision to export: $x_{it} = \{0, 1\}$

$$V_t = \max E_t \sum_{s=t}^{\infty} \frac{1}{1 + r_s} x_{is} \left(\pi_{is} (\cdot) - f_{is}(\cdot) \right)$$

- Fixed export costs: $f_{it} \left(\epsilon_{it}, x_{it-1}, x_{it-2}, ..., x_{it-k} \right)$ depend on random variable and experience
- Flow profits: $\pi \left(x_{it}, z_{it}, d_{it} \right)$
  - z_{it} = variables related to productive efficiency
  - d_{it} = variables related to foreign demand for firm i's good
  - Assumes constant returns to scale, otherwise $z_{it} \left(s_{it}, d_{it} \right)$ where s_{it} is sales at home

Foreign demand

- Assume a firm charging price p_{it} sells

$$d_{it}\left(p_{it}\right) = \omega_{it}\left(p_{it}\frac{\tau_t \xi_t \tilde{\xi}_{it}}{P_t}\right)^{-\theta} D_t$$

- Common factors: market size (D_t), real exchange rate (P_t), ad-valorem tariff (τ_t), iceberg trade costs (ξ_t)
- Idiosyncratic factors: demand shifter (ω_{it}) and $\left(\tilde{\xi}_{it}\right)$ e.g., shipping/distribution technology
  - Two idiosyncratic factors redundant, combine into ξ_{it}
  - No congestion effects on distribution
- CES framework is common

Fixed costs

- Following Baldwin and Krugman (1989); Roberts and Tybout (1997)
- $f(\epsilon_{it}, x_{it-1})$: only $t-1$ export status matters (full depreciation of market-access investment)
- $f(\epsilon_{it}, 1) < f(\epsilon_{it}, 0)$: cost of entering exceeds continuation cost (upfront investment in market access)
- fixed cost lowers iceberg cost from $\xi = \infty$ to $\xi < \infty$ (return on investment)
- When fixed trade cost only depends on last period's export status the fixed cost and history variable are redundant.
- A richer model in which fixed costs depend on experience requires tracking longer history

Uncertainty

- Microeconomic $(z, \xi, f(\epsilon_{it}, x_{it-1}))$
  - Let z, ξ follow AR1 process $\left(\rho_z, \sigma_z^2, \rho_\xi, \sigma_\xi^2\right)$
  - Fixed cost component follow $\epsilon_{it} \sim \log \text{Normal}\left(0, \sigma_\epsilon^2\right)$
  - Often assume aspect of ξ is learned upon entry (Learning)
- Macroeconomic
  - Processes for exchange rate (P_t) & demand (D_t) depend on equilibrium concept
  - In partial equilibrium (P, D) are exogenous AR processes
  - In general equilibrium, (P, D) depend on shocks and transmission (can be highly non-linear)
  - For tariffs no standard

Bellman Equation

- The firm solves a standard discrete-choice problem

$$V_t\left(x_{it-1}, z_{it}, \xi_{it}, f_{it}\right) = \max\left\{ V_t^0\left(x_{it-1}, z_{it}, \xi_{it}, f_{it}\right), V_t^1\left(x_{it-1}, z_{it}, \xi_{it}, f_{it}\right)\right\}$$

- To solve this problem we will need to know
  - A firm's survival probability (δ_{it})
  - The interest rate (r_t)
- The ts capture non-stationary functions from aggregate shocks
  - Most partial equilibrium models assume stationarity

Bellman Equation

- Value of not exporting

$$\begin{aligned} V_t^0\left(x_{it-1}, z_{it}, \xi_{it}, f_{it}\right) &= \pi_t\left(0, z_{it}, \xi_{it}\right) \\ &\quad +\delta_{it} \underset{z,\xi,f}{\mathrm{E}} \frac{1}{1+r_{t+1}} V_{t+1}\left(0, z_{it+1}, \xi_{it+1}, f_{it+1}\right) \end{aligned}$$

- Value of exporting

$$\begin{aligned} V_t^1\left(x_{it-1}, z_{it}, \xi_{it}, f_{it}\right) &= \pi_t\left(1, z_{it}, \xi_{it}\right) - f(\epsilon_t, x_{i,t-1}) \\ &\quad +\delta_{it} \underset{z,\xi,f}{\mathrm{E}} \frac{1}{1+r_{t+1}} V_{t+1}\left(1, z_{it+1}, \xi_{it+1}, f_{it+1}\right) \end{aligned}$$

- Focus on a stationary environment for now (drop ts)

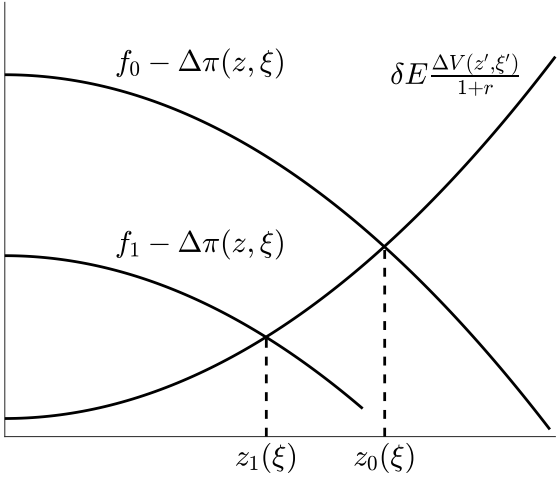
Decision Rules

- Assume 1) f is deterministic (i.e. $\sigma_\epsilon = 0$) and 2) export and domestic profit increasing in z
- Optimal policy is a cutoff rule $z_m(\xi)$ s.t. $x_{it} = 1$ iff $z \geq z_m(\xi)$

$$
\begin{aligned}
f_m - \left[\pi\left(1, z_m(\xi), \xi\right) - \pi\left(0, z_m(\xi), \xi\right)\right] &= \frac{\delta}{1+r} E\left[\begin{array}{c} V^1\left(z', \xi', f_1\right) \\ -V^0\left(z', \xi', f_0\right) \end{array}\right] \\
f_m - \Delta\pi\left(z_m(\xi), \xi\right) &= \frac{\delta}{1+r} E\left[\Delta V\left(z', \xi', f_1, f_0\right)\right]
\end{aligned}
$$

- The LHS is the current cost of exporting net of increased profits
- The RHS is the future benefit (increase in market value of the firm)

Breakevens (for a realization of ξ)



The gain in firm value from exporting

- The RHS of the break-even condition
- The upward sloping line in the figure
- Depends on fixed costs and persistence of shock
- The slope is increasing in the persistence of shocks
  - It determines both how long and how much you earn exporting
- The intercept is mostly determined by the gap between $f_0 - f_1$
  - If $f_0 = f_1$ then $\Delta V = 0$
  - Holding f_1 constant, $\frac{\partial \Delta V}{\partial f_0} > 0$

The current cost of exporting

- The LHS of the break-even condition
- The downward sloping lines in the figure

- Holding fixed ξ cost decreases in z
  - Exporting more profitable to more productive firms

Distributions

- The cutoff thresholds and the process for (z, ξ) determine the measure of firm types $\mu(z, \xi, f)$
- $\mu(z, \xi, f_0)$ [$\mu(z, \xi, f_1)$] denotes the beginning of period non-exporters [exporters]
- The measures of current nonexporters and exporters

$$N_N = \int_{\xi} \int_{0}^{z_0(\xi)} \mu(z, \xi, f_0) + \int_{\xi} \int_{0}^{z_1(\xi)} \mu(z, \xi, f_1)$$

$$N_X = \int_{\xi} \int_{z_0(\xi)}^{\infty} \mu(z, \xi, f_0) + \int_{\xi} \int_{z_1(\xi)}^{\infty} \mu(z, \xi, f_1)$$

- The export participation share is $N_X / (N_N + N_X)$

Laws of motion

$$N'_X = \delta_{X,X} \Pr(\text{continue}) N_X + \delta_{N,X} \Pr(\text{start}) N_N$$

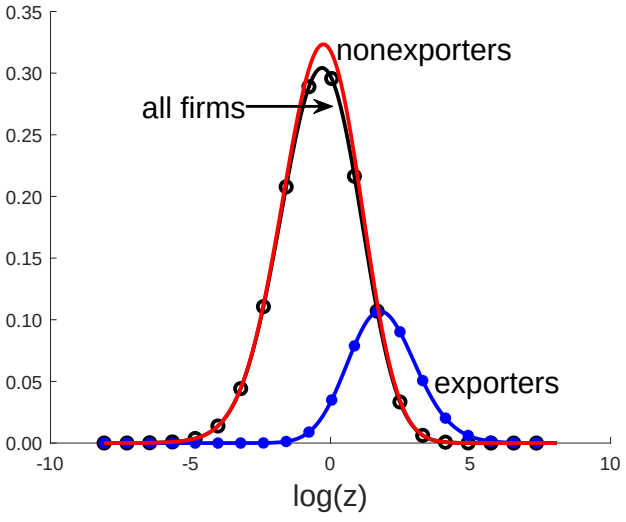
$$N'_N = \delta_{X,N} [1 - \Pr(\text{continue})] N_X + \delta_{NN} [1 - \Pr(\text{start})] N_N + N_E$$

- A more careful exposition would focus fully on

$$\mu'(z, \xi, f) = T(\mu(z, \xi, f))$$

- See the appendix to Alessandria et al. (2021a) for details

Distributions



Properties

- Crucial outcome of dynamic decision: $z_1(\xi) < z_0(\xi)$
  - Harder to break into exporting than to stay
- This generates
  - **Exporter hysteresis:** Firms continue exporting after conditions deteriorate
  - **Low exit rate:** Exporters will delay exiting to avoid paying the entry cost again
  - **Export Premium:** Exporters are larger than nonexporters
    - Increasing in the average fixed cost
    - Falling in the difference in fixed costs

Properties

- Consider the impact of changes in current and future primitives abstracting from GE interactions
- Let's look at
  1. Trade barriers
  2. Uncertainty

Trade costs and Tariffs

- Consider three possible reductions in variable trade costs, either (ξ, τ)
  1. Current trade costs temporary
  2. Future trade costs permanent
  3. Current and future trade costs

Temporary current

- Experiment: $\tau_t \downarrow$, $\tau_s = \tau_{t-1}$, $s = t+1, t+2, \ldots$
- Tariff cut is a surprise
- Lowering today's tariff will shift down the $\text{LHS}_m(z)$
- Increasing entry and decreasing exit
- Through law of motion, trade will remain persistently high, only gradually mean-reverting

Permanent future

- Lowering tariff in the future will shift up the $\text{RHS}_m(z)$
- Increasing entry and decreasing exit today
- Trade grows in advance of liberalization
- Through law of motion trade will increase gradually

Permanent current

- Lowering tariff in the current will shift up the $\text{RHS}_m(z)$ and $\text{LHS}_m(z)$
- Combination of previous two shocks
- Increasing entry and decreasing exit today
- Trade grows by more on impact
- Through law of motion trade will increase gradually.

Uncertainty

- As in typical models with non-convexities, uncertainty matters (Dixit and Pindyck, 1994)

1. Current dispersion in productivity, $\sigma_z \uparrow$ [temporary]
   - Does not affect thresholds, but does affect distribution of ability today
   - Thicker tails $\rightarrow$ more entry and more exit
   - Volume of trade should increase since conditional mean of productivity $\uparrow$ (selection on a thicker right tail)

2. Future uncertainty/dispersion, $\sigma_z' \uparrow$ [permanent]
   - Shift up and flattening of the marginal gain curve
   - Entry and exit fall, ambiguous effect on trade today and in the future

Success and Challenges

- Successes
  - Persistent export participation (fact #1)
  - Low export and entry rates (facts #3,4)
  - Dynamic macro adjustment (fact #7)
- Challenges
  - New exporters (too productive at entry, too likely to continue, export intensity too high)
  - Connection in exporting across markets
  - High re-entry rates in monthly and longer frequencies
- Causes
  - Exporting technology too simple (parsimonious): f_0, f_1, ξ
  - Need to shift more investment into post-entry period and reduce depreciation

Resolutions: Starting and stopping

- Small new-exporters & low continuation rate
  - Let $f_1(t_e)$ be a decreasing function of t_e=age in market
- High re-entry data
  - Annual: Let firm that stops re-enter with $f_R \in [f_1, f_0]$
  - Monthly: set $f_0 = f_1$, hold goods in inventories at a cost abroad

Resolution: Export intensity dynamics

With CES

$$exs(z, \hat{\xi}) = \frac{(\tau \xi \hat{\xi})^{1-\sigma}}{1 + (\tau \xi \hat{\xi})^{1-\sigma}}$$

- Modify iceberg cost structure so that they fall with experience
  - Alessandria et al. (2021b) assume firm enters at $\xi_H > \xi_L$ and then Markov transition between states
  - Reflects improvements in export distribution technology
- Alternatively could accumulate customers or build habit (Fitzgerald et al., 2016; Piveteau, 2021; Ruhl and Willis, 2017; Rodrigue and Tan, 2019)
- Both approaches have investments in improving market after entry, not just maintaining access
- Backloads profits which leads to lower estimates of entry costs.
- When growth process is uncertain, this makes it more likely to exit

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